

Computing below the expected energy limits

Luca Gammaitoni

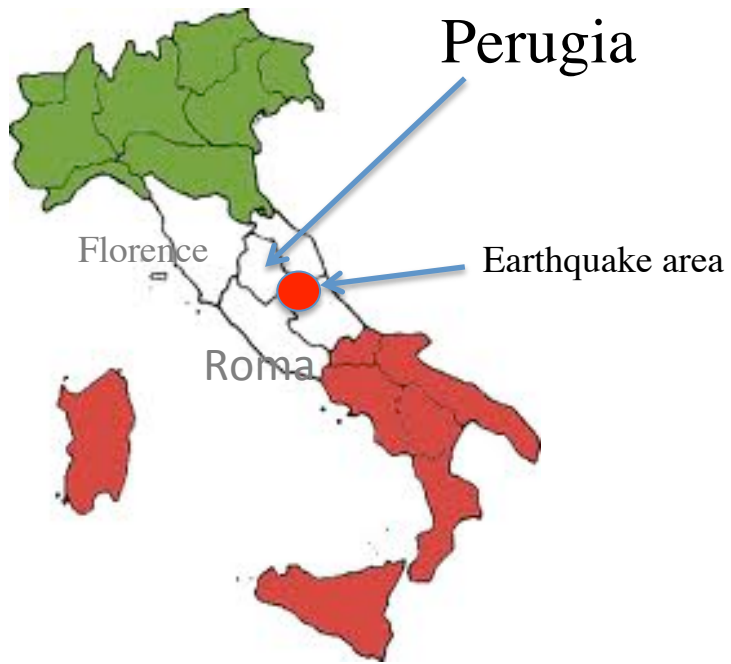
NiPS Laboratory, University of Perugia

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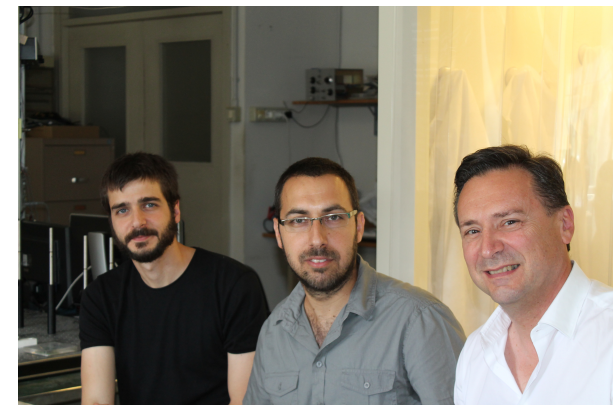
AD 1308



NiPS Laboratory
Noise in Physical Systems



2016 (13 FT, 1 PT)



M. Lopez-Suarez, I. Neri, L.G.

E.C. FET Proactive GA Landauer 318287
ONRG grant N00014-11-1-0695



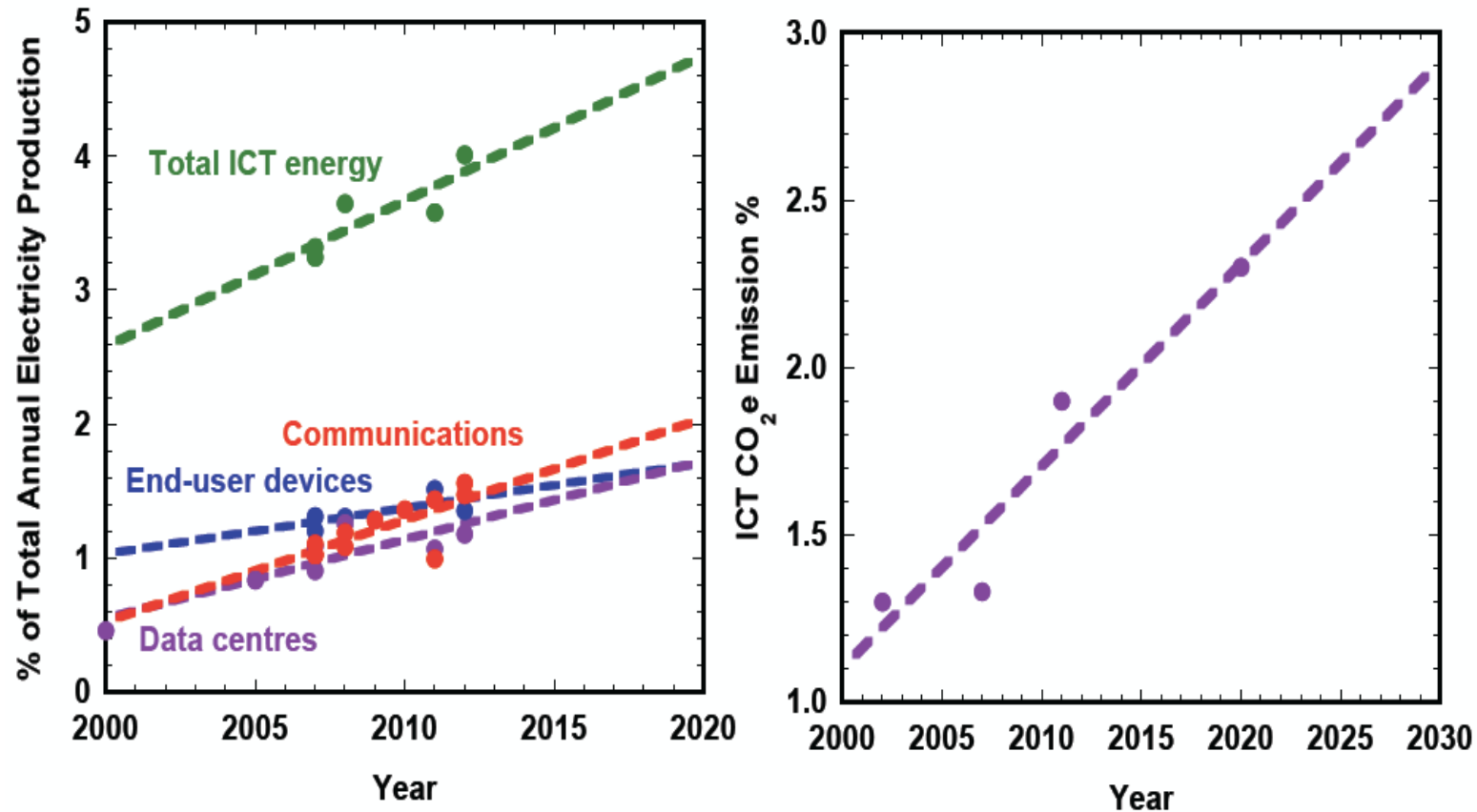
Present computers are energy hungry

April 4,
2005



March 13,
2013

ICT global energy consumption

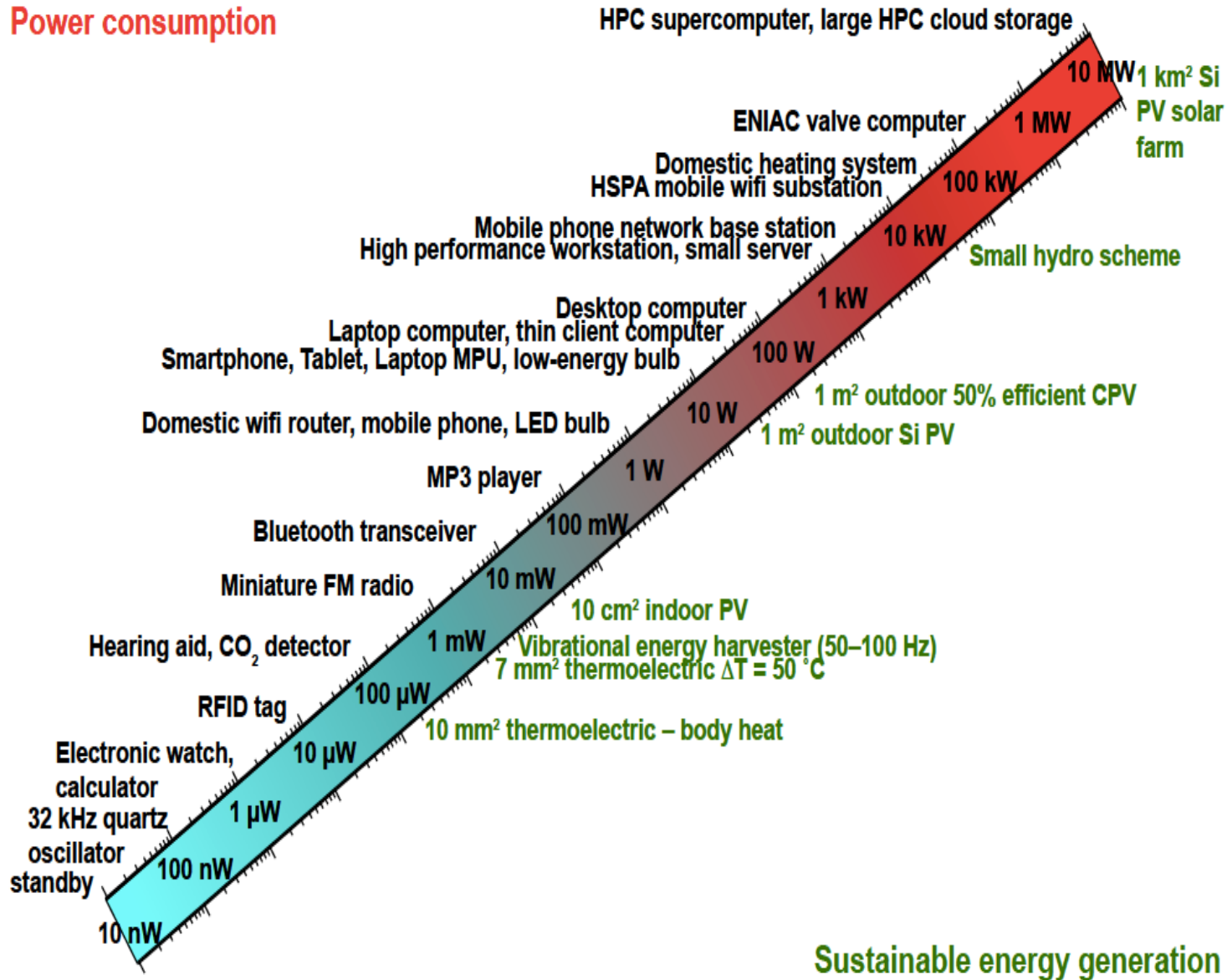


This excludes TV, media, publishing, games, power switches, domestic & industrial ICT devices

Source: D. Paul, ICT-Energy Research Agenda, 2015

ICT energy requirements

Power consumption



Source: D. Paul, ICT-Energy Research Agenda, 2015

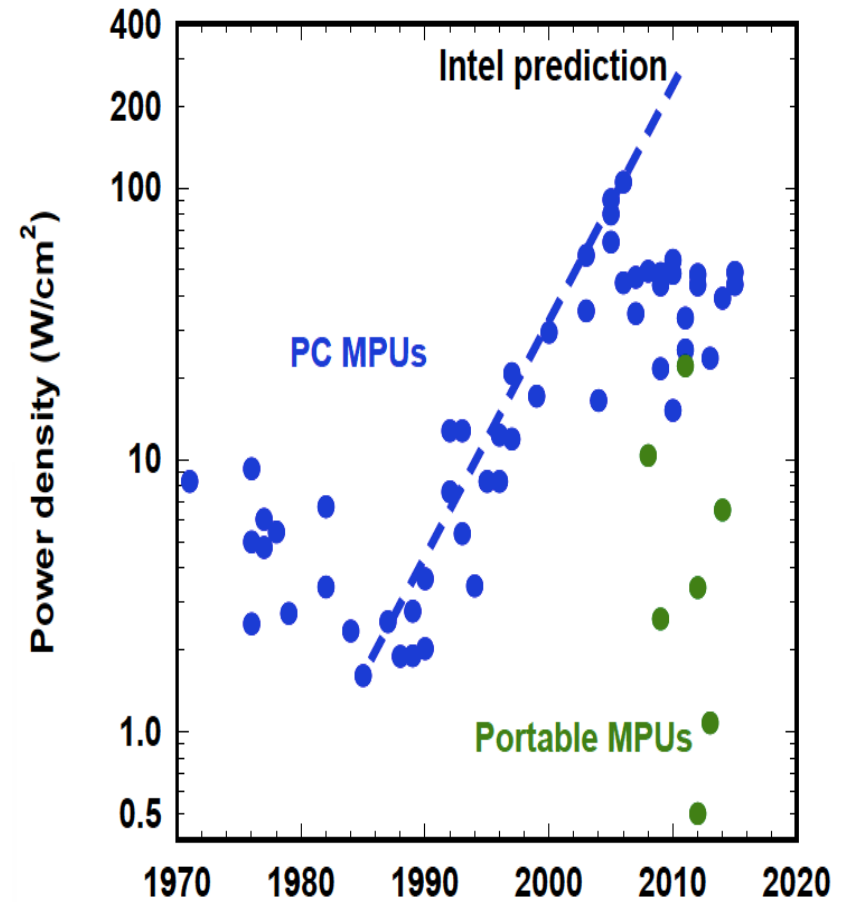
Sustainable energy generation

Reducing energy is strategic

If we want more powerful supercomputers



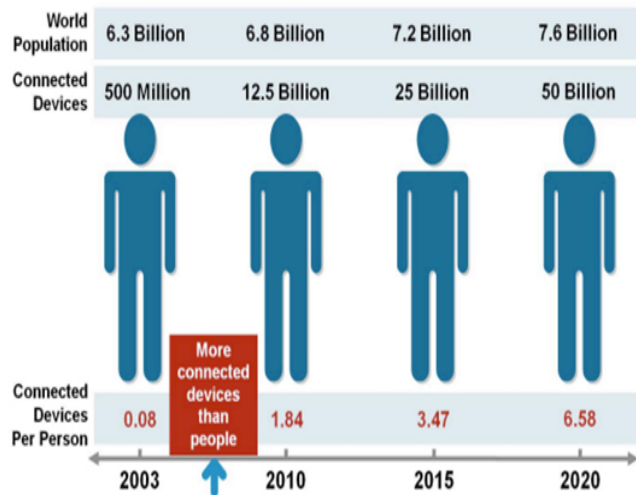
...to avoid microprocessor burning



Source: D. Paul, ICT-Energy Research Agenda, 2015

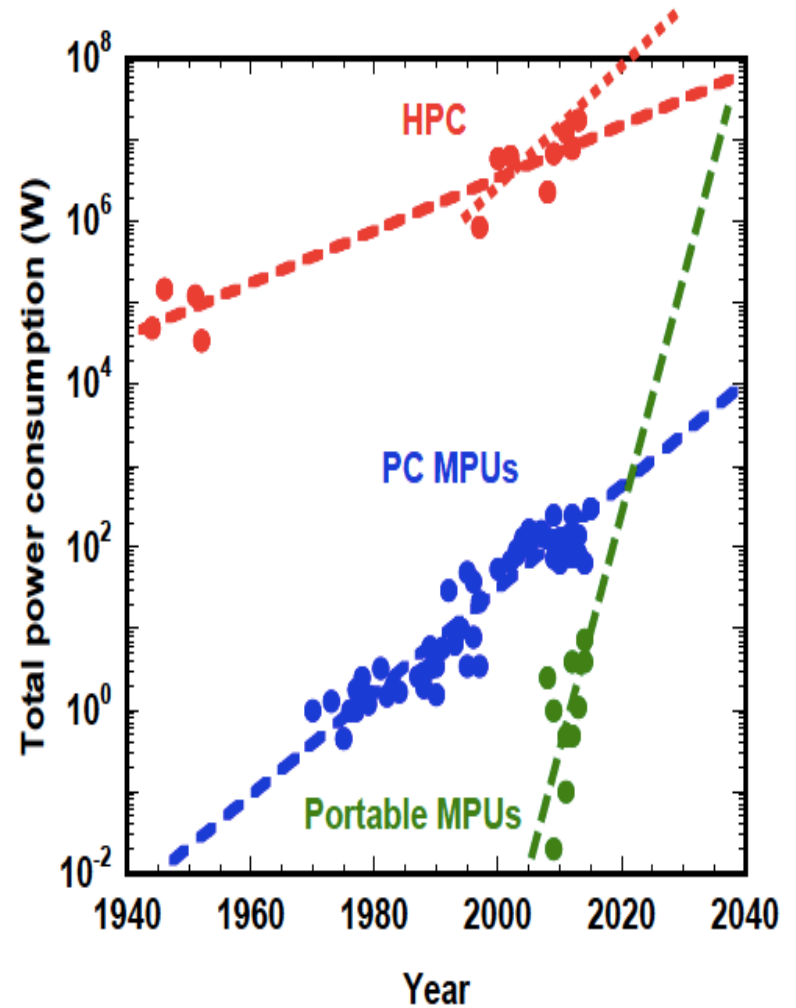
Reducing energy is strategic

If we want the **Internet of Things** to happen



Source: Cisco IBSG, April 2011

...to avoid lacking autonomous power



Source: D. Paul, ICT-Energy Research Agenda, 2015

What can we do?



If I could build any machine for doing computing, what is going to be the minimum energy required to do computation with it?

Can we design computers that are operated without spending any energy?

Computers are physical systems that process information while changing work into heat



By the moment that information processing/computing can be associated with the change of bits, in order to perform this activity we need two very important ingredients:

- a) a physical system capable of assuming two different physical states: S_0 and S_1
- b) a set of forces that induce state changes in this physical system:
 - F_{01} produces the change $S_0 \rightarrow S_1$
 - F_{10} produces the change $S_1 \rightarrow S_0$.

A simple system to perform computation



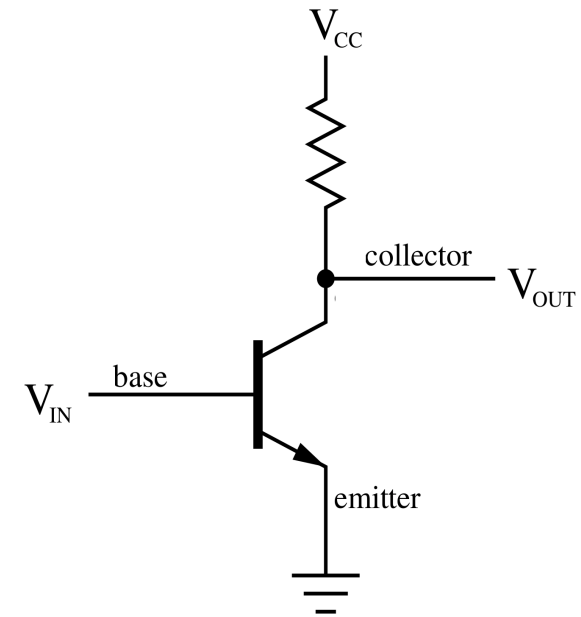
the physical system, made by a pebble* and two bowls.

- a) The two states are represented by the measurable quantity “position of the pebble”:
state “0” = pebble in left bowl; state “1” = pebble in right bowl;
- b) the way to induce state changes represented by a force that brings around the pebble.

* “Calculus” is the Latin word for pebble

Devices that obeys the rules a) and b) are called *binary switches*.

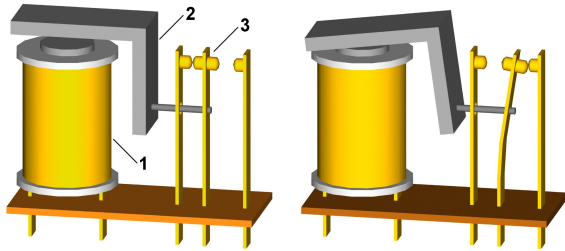
In modern computers binary switches are made with transistors. These are electronic devices that satisfy the two conditions required:



- a) The two states are represented by the measurable quantity “electric voltage” at point V_{OUT} . As an example state “0” = $V_{OUT} < V_T$; state “1” = $V_{OUT} > V_T$; with V_T a given reference voltage.
- b) The way to induce state changes represented by an electromotive force applied at point V_{IN} .

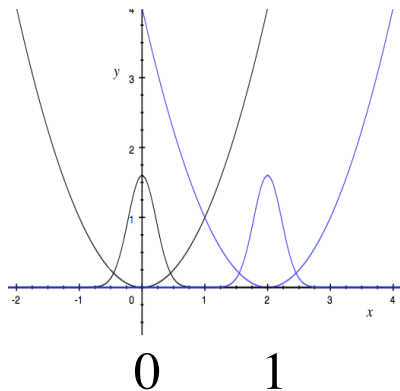
Binary switches

There exist at least two classes of devices that can satisfy the rules a) and b). We call them *combinational* and *sequential* devices.



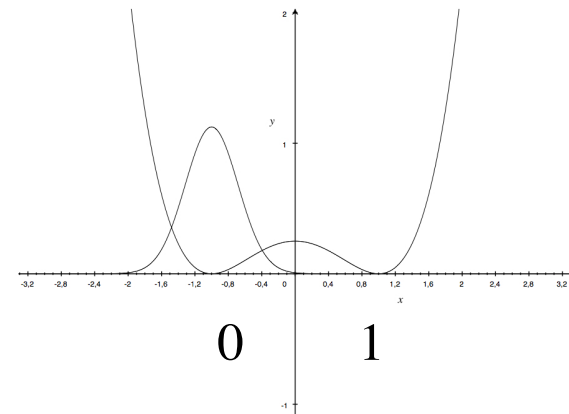
Combinational:

in the absence of any external force, under equilibrium conditions, they are in the state S_0 . When an external force F_{01} is applied, they switch to the state S_1 and remain in that state as long as the force is present. Once the force is removed they go back to the state S_0 .



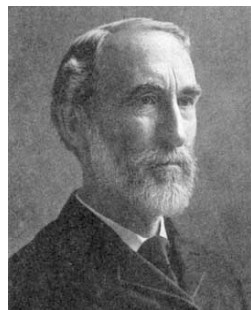
Sequential:

They can be changed from S_0 to S_1 by applying an external force F_{01} . Once they are in the state S_1 they remain in this state even when the force is removed. They go from S_1 to S_0 by applying a new force F_{10} . Once they are in S_0 they remain in this state even when the force is removed.



Questions

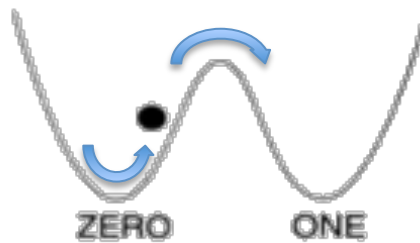
- What is the minimum energy we have to spend if we want to produce a switch event ?
- Does this energy depends on the technology of the switch ?
- Does this energy depends on the instruction that we give to the switch ?
-



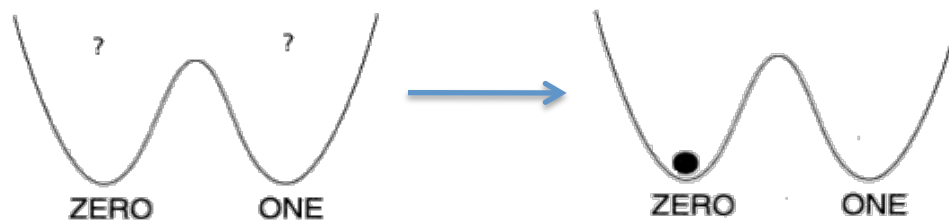
There are two basic operations we can do with a sequential switch



The switch operation (i.e. the change of state)

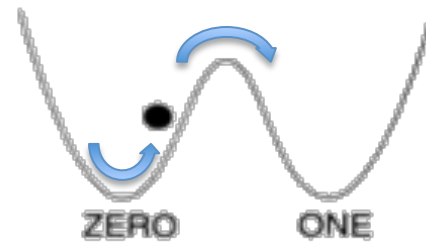


The reset operation (i.e. the set of a given state starting from an unknown state)



Let's look at this, with a reasoning introduced in 1961 by R. Landauer

The single switch operation



0 → 1

Before the switch = 1 logic state

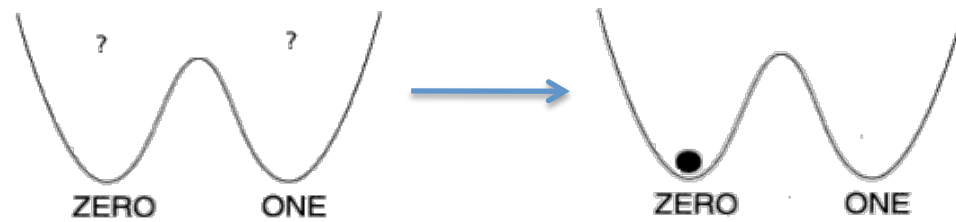
After the switch = 1 logic state

$$\text{Change in entropy} = S_f - S_i = K_B \log(1) - K_B \log(1) = 0$$

No net decrease in entropy ---> no minimum energy required



The reset operation



? \longrightarrow 0

Before the reset = 2 possible logic states

After the reset = 1 logic state

Change in entropy = $S_f - S_i = K_B \log(1) - K_B \log(2) = -K_B \log(2)$

Net decrease in entropy \longrightarrow **energy expenditure required**



THE VON NEUMANN-LANDAUER BOUND

The Landauer's principle (1) states that erasing one bit of information (like in a resetting operation) comes unavoidably with a decrease in physical entropy and thus is accompanied by a minimal dissipation of energy equal to

$$Q = k_B T \ln 2$$

More technically this is the result of a change in entropy due to a change from a random state to a defined state.

Please note: this is the **minimum** energy required.



(1) R. Landauer, "Dissipation and Heat Generation in the Computing Process"
IBM J. Research and Develop. 5, 183-191 (1961),

LOGICAL REVERSIBILITY

In the same paper Landauer generalized this result associated with the reset operation to the cases where there was a decrease of information between the input and the output of a computing system.

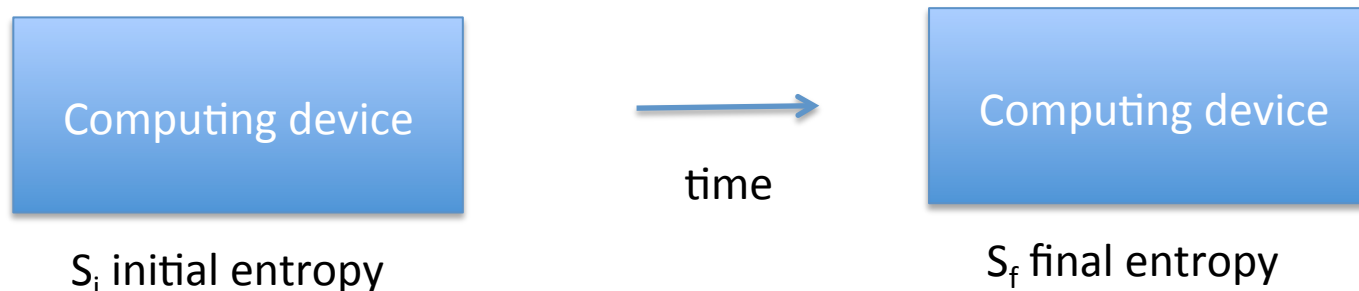
Landauer wrote:



*We shall call a device logically irreversible if the output of a device does not uniquely define the inputs. We believe that devices exhibiting logical irreversibility are essential to computing. Logical irreversibility, we believe, in turn **implies** physical irreversibility, and the latter is accompanied by **dissipative effects**.*

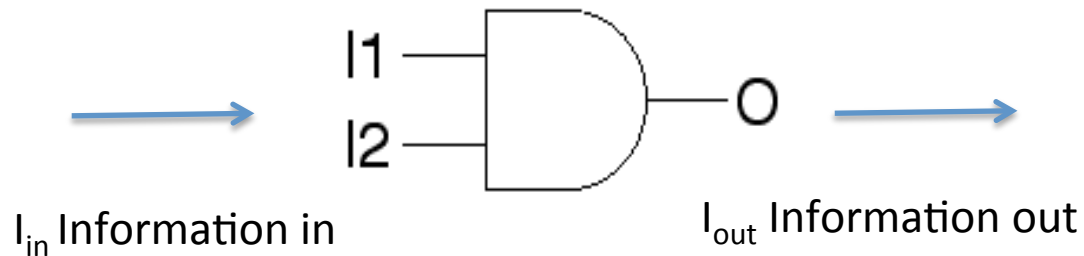


Change of paradigm: the Boltzmann thermodynamics was:



TRADITIONAL COMPUTING

Logically irreversible $I_{\text{out}} < I_{\text{in}}$



Logically reversible COMPUTING ($I_{\text{out}} = I_{\text{in}}$)

Bennet wrote:

Landauer has posed the question of whether logical irreversibility is an unavoidable feature of useful computers, arguing that it is, and has demonstrated the physical and philosophical importance of this question by showing that whenever a physical computer throws away information about its previous state it must generate a corresponding amount of entropy.

*Therefore, a computer **must dissipate** at least $k_B T \ln 2$ of energy (about 3×10^{-21} Joule at room temperature) for each bit of information it erases or otherwise throws away.*

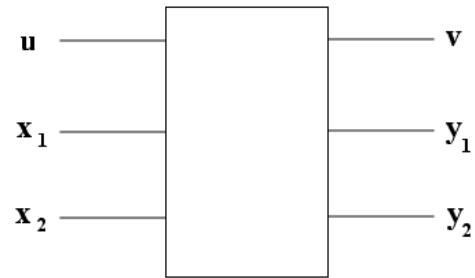


C. H. Bennett, "Logical reversibility of computation," IBM Journal of Research and Development, vol. 17, no. 6, pp. 525-532, 1973.

LOGICALLY REVERSIBLE GATES



E. Fredkin



$$v = u$$

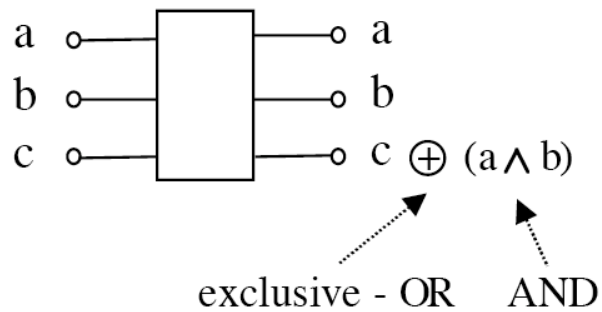
$$y_1 = u x_1 + u' x_2$$

$$y_2 = u' x_1 + u x_2$$



B. Toffoli

Toffoli gate



When and only when a and b are 1's, c is inverted.

CONTROVERSIAL RESULT

PROCEEDINGS OF THE ROYAL SOCIETY A MATHEMATICAL, PHYSICAL & ENGINEERING SCIENCES

Information erasure without an energy cost
Joan A. Vaccaro and Stephen M. Barnett
Proc. R. Soc. A 2011 **467**, doi: 10.1098/rspa.2010.0211
12 January 2011

Waiting for Landauer
John D. Norton¹
Department of History and Philosophy of Science, Center for Philosophy of Science, University of Pittsburgh, USA

Beyond Landauer Erasure
Stephen M. Barnett¹ and Joan A. Vaccaro^{2,*}

Minimal Energy Cost for Thermodynamic Information Processing: Measurement and Information Erasure
Takahiro Sagawa and Masahito Ueda
Phys. Rev. Lett. **102**, 250602 – Published 24 June 2009; Erratum Phys. Rev. Lett. **106**, 189901 (2011)

Studies in History and Philosophy of Modern Physics 42 (2011) 184–198
Contents lists available at ScienceDirect
ELSEVIER
journal homepage: www.elsevier.com/locate/shpsb

Entropy 2013, 15, 4956–4968; doi:10.3390/e15114956
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ISSN 1099-4308

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EXPERIMENTS

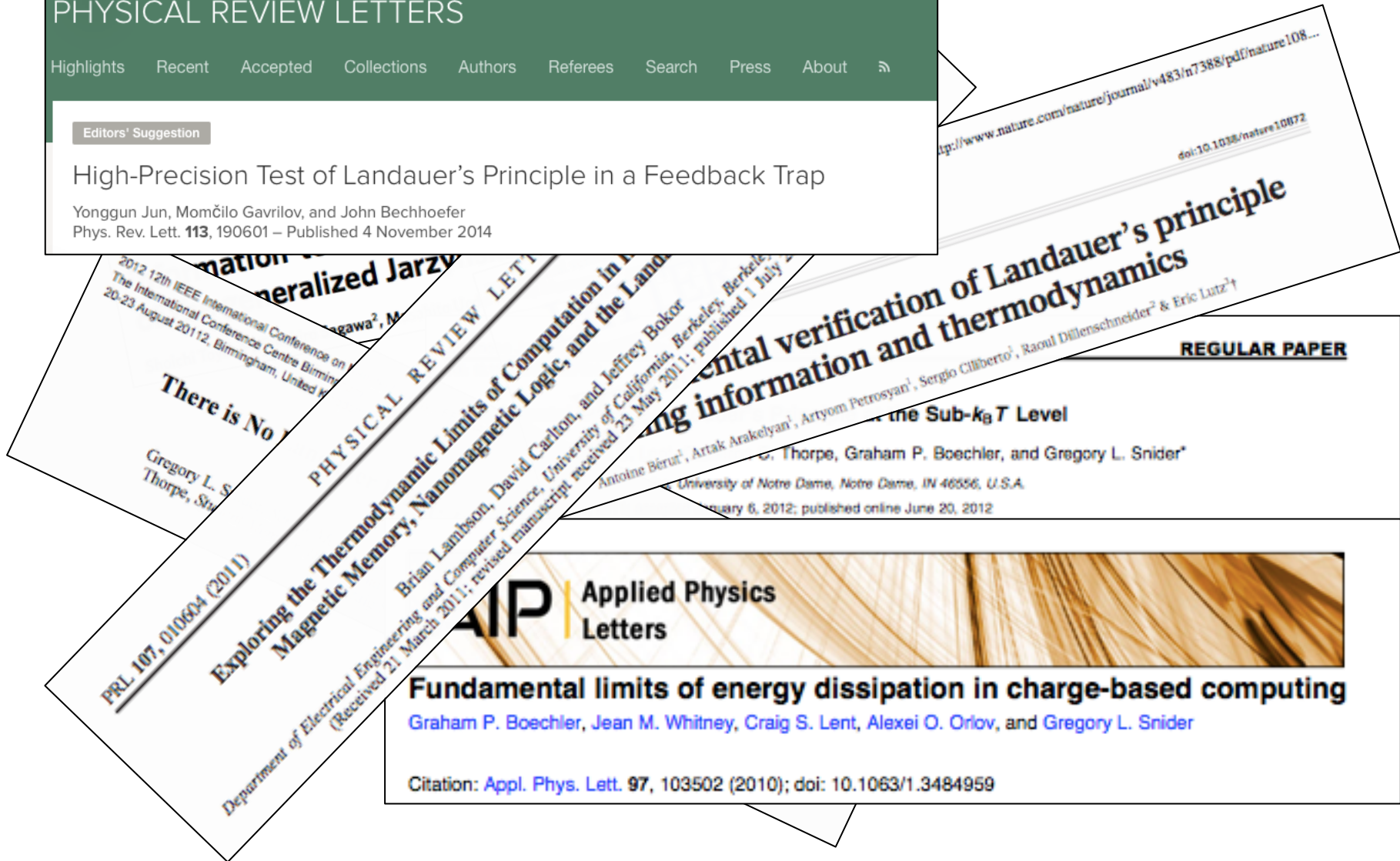
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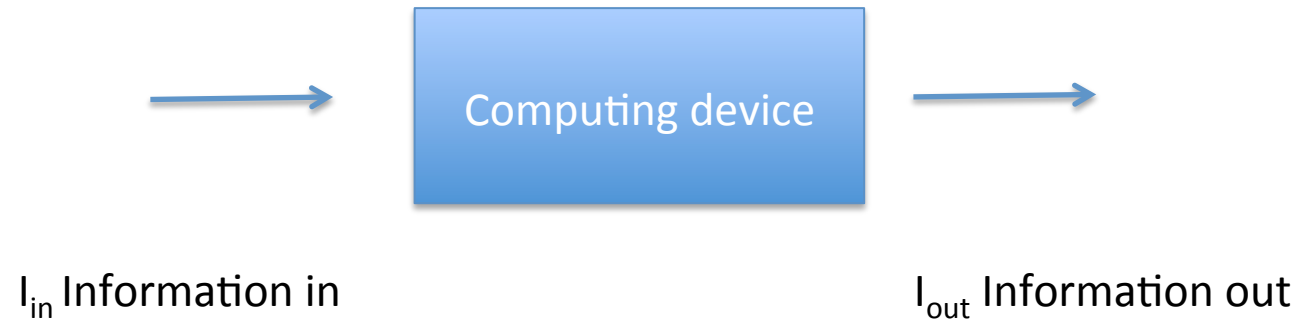
Editors' Suggestion

High-Precision Test of Landauer's Principle in a Feedback Trap

Yonggun Jun, Momčilo Gavrilov, and John Bechhoefer
Phys. Rev. Lett. **113**, 190601 – Published 4 November 2014

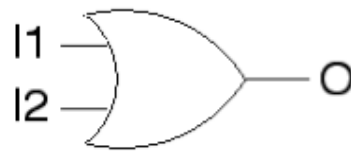


Testing the logical irreversibility limit



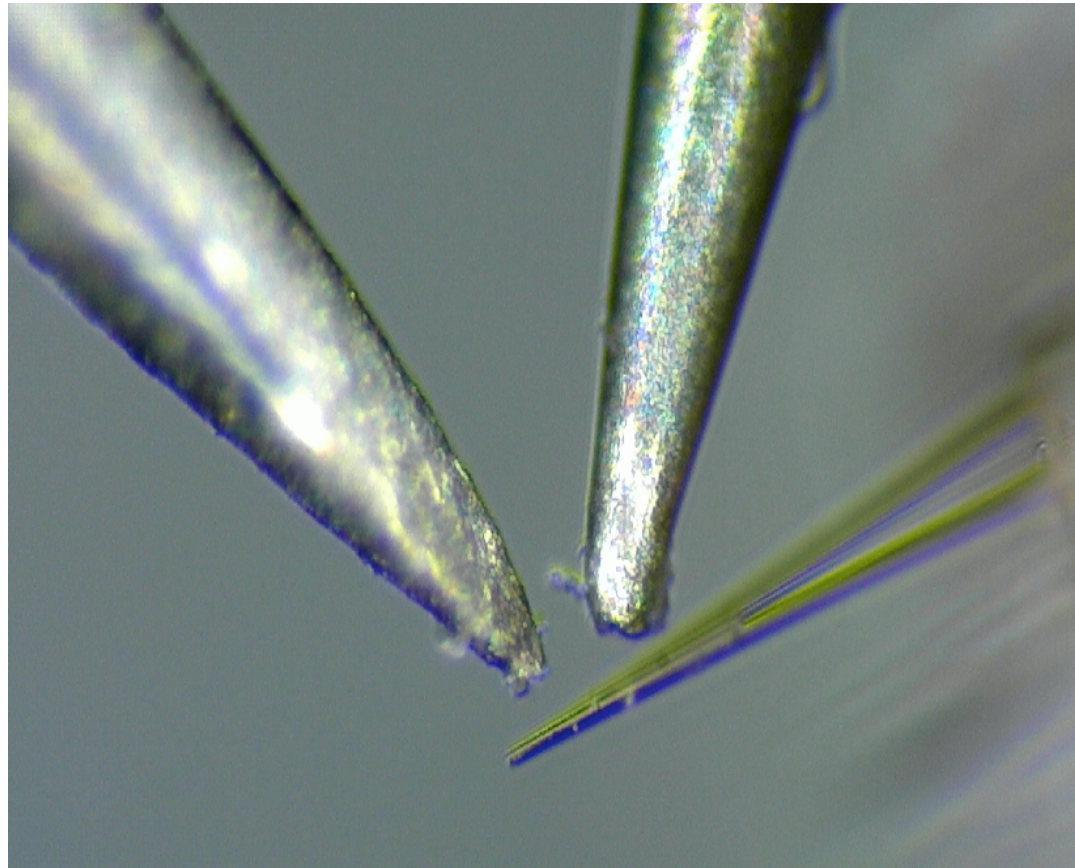
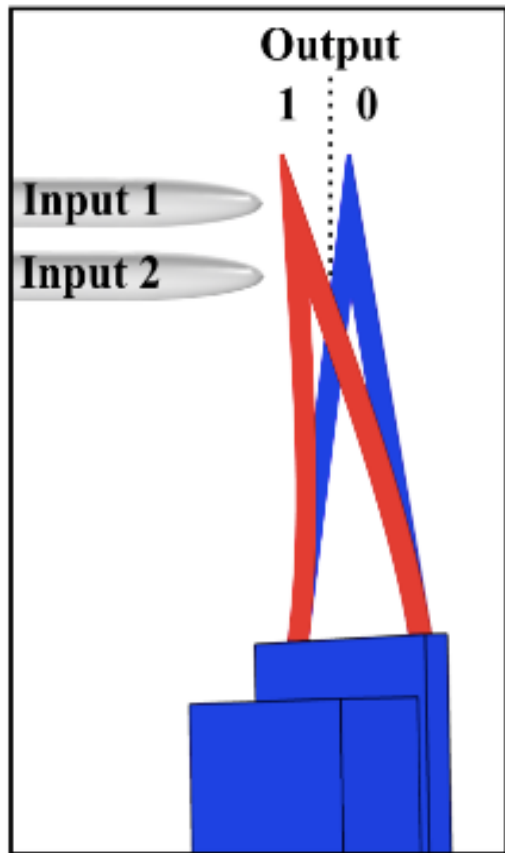
Logical irreversibility: $I_{out} < I_{in}$

OR

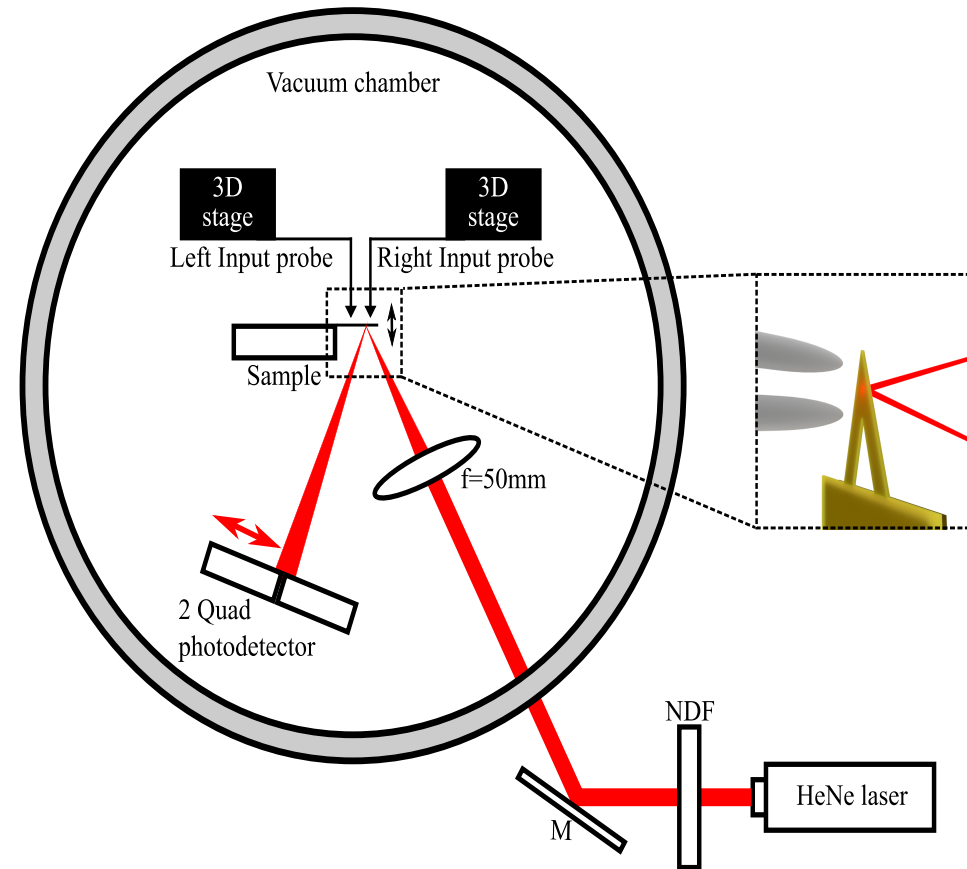
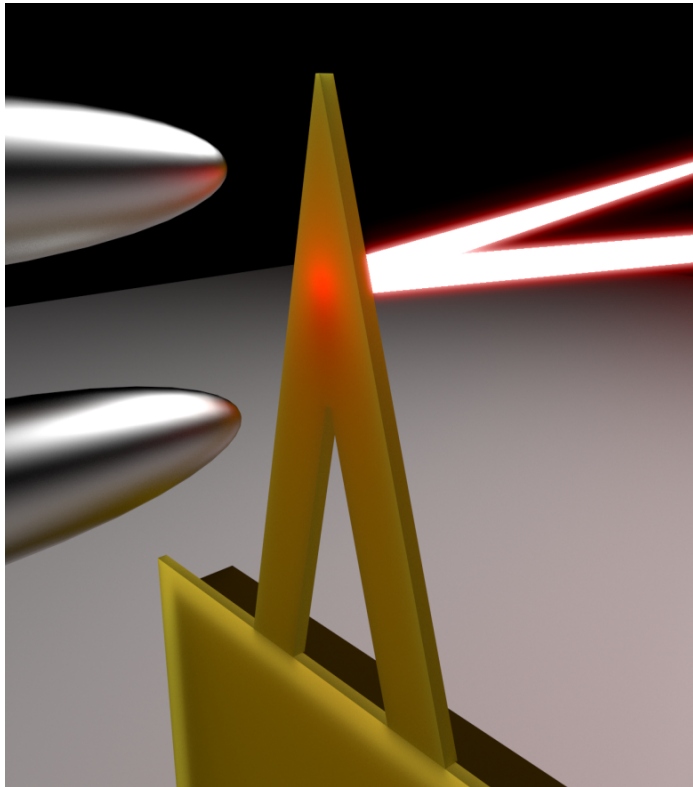


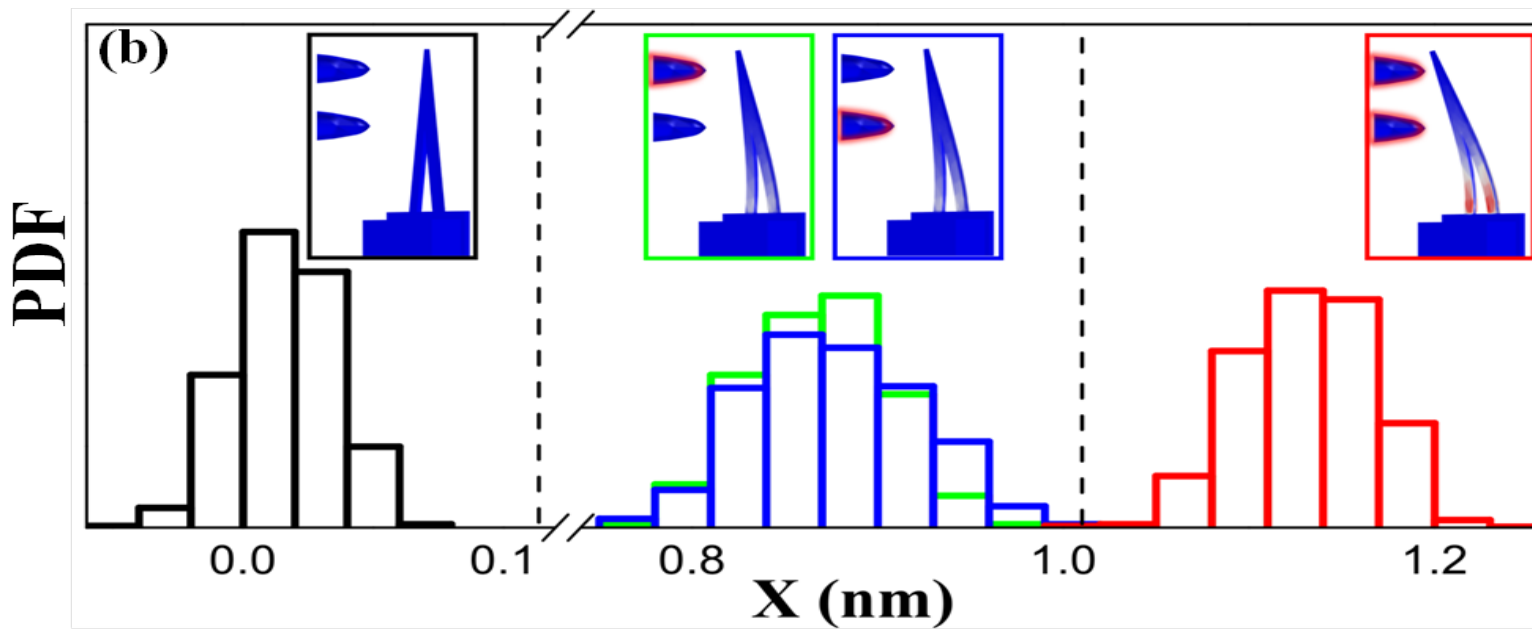
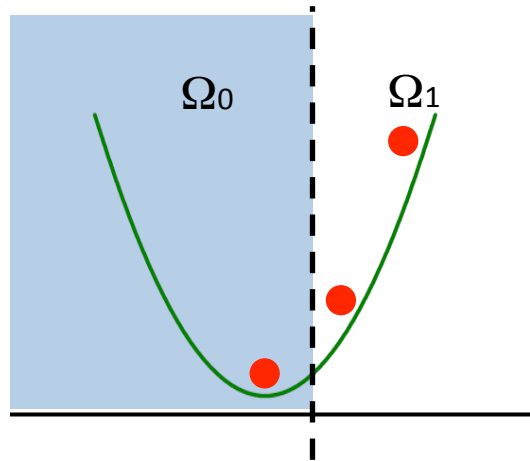
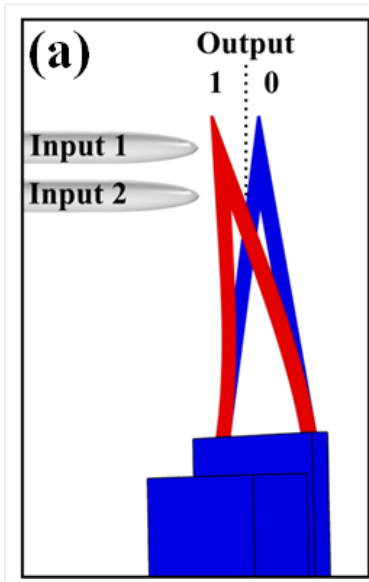
I_1	I_2	O
0	0	0
0	1	1
1	0	1
1	1	1

Micro electro-mechanical Logic gate

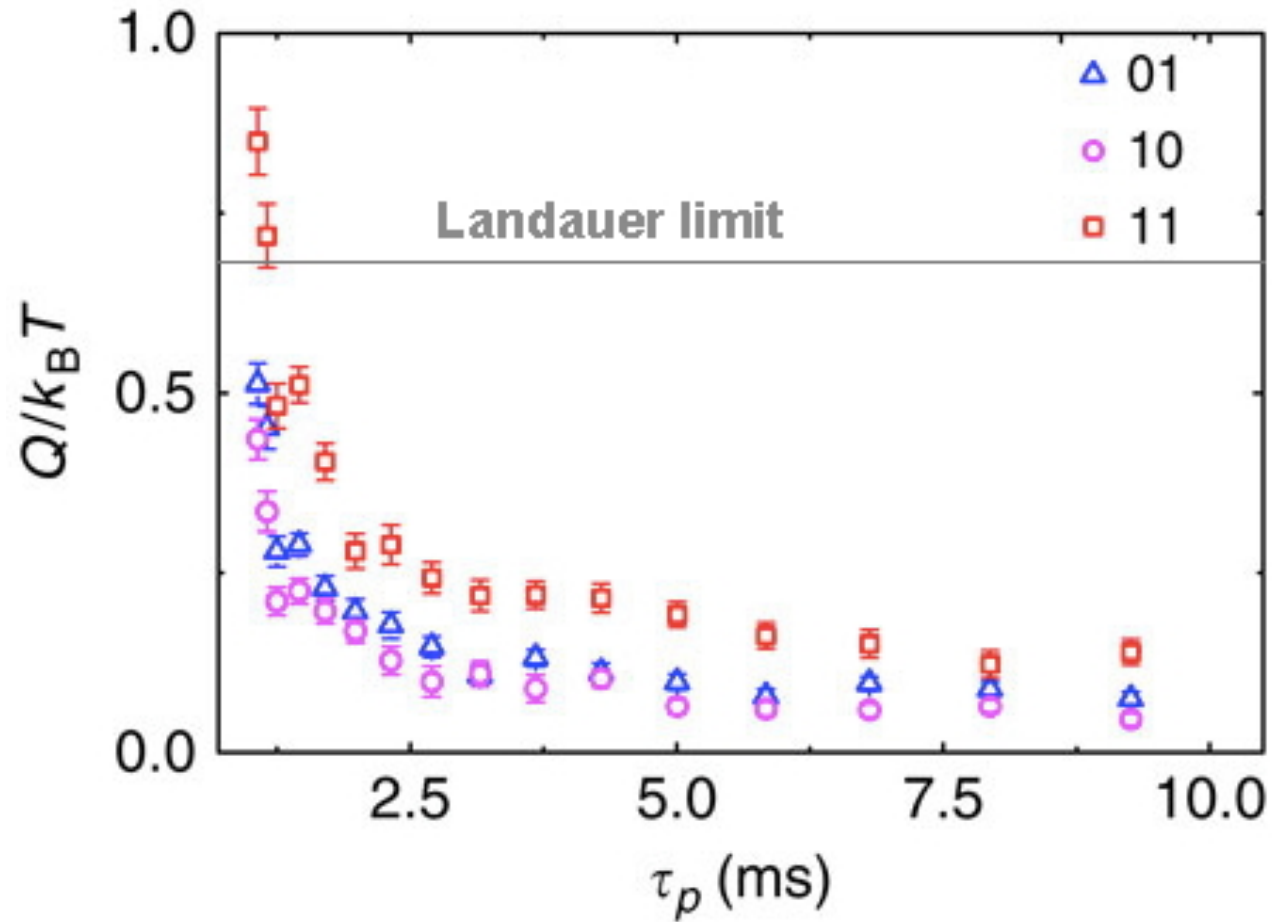


Micro electro-mechanical Logic gate



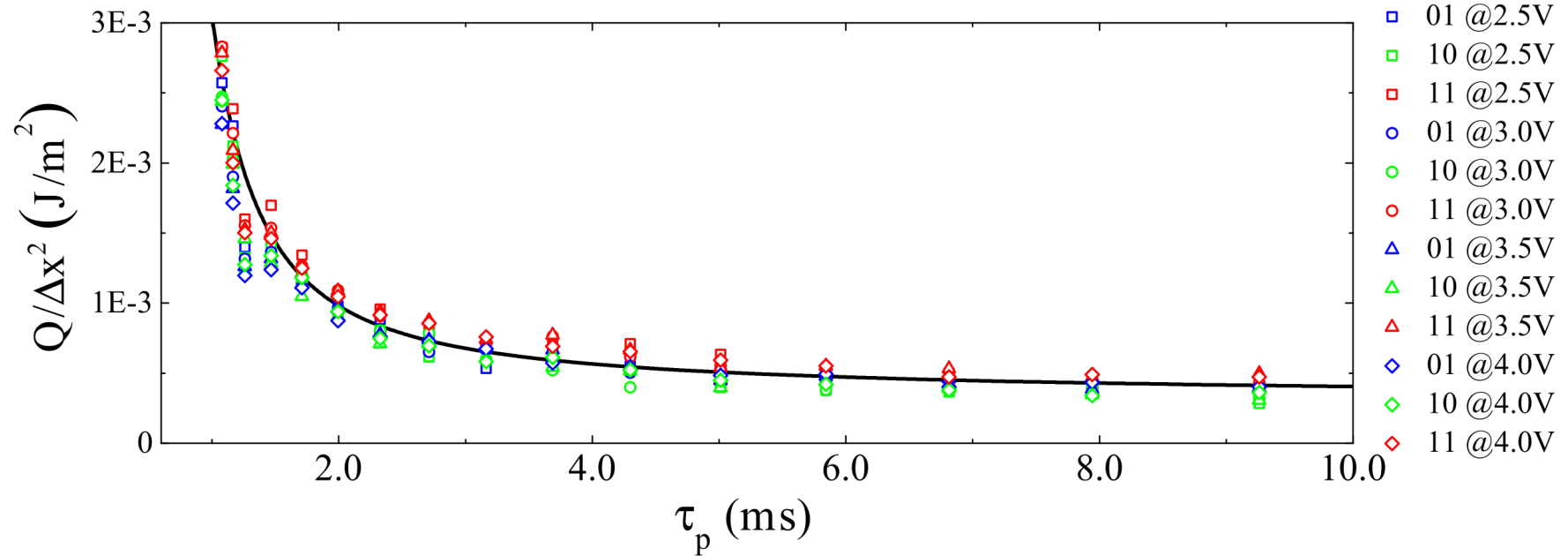


Measure of the energy dissipated during information processing with OR logic gate



Sub-kBT micro-electromechanical irreversible logic gate,
M. López-Suárez, I. Neri, L. Gammaitoni.
Nature Communications 7, Article number: 12068 (2016)

Dissipation model



Zener theory $-k(1 + i\phi)$

$$\phi(v) = \phi_{\text{str}} + \phi_{\text{th-el}} + \phi_{\text{vis}} + \phi_{\text{clamp}}$$

LOGICAL REVERSIBILITY

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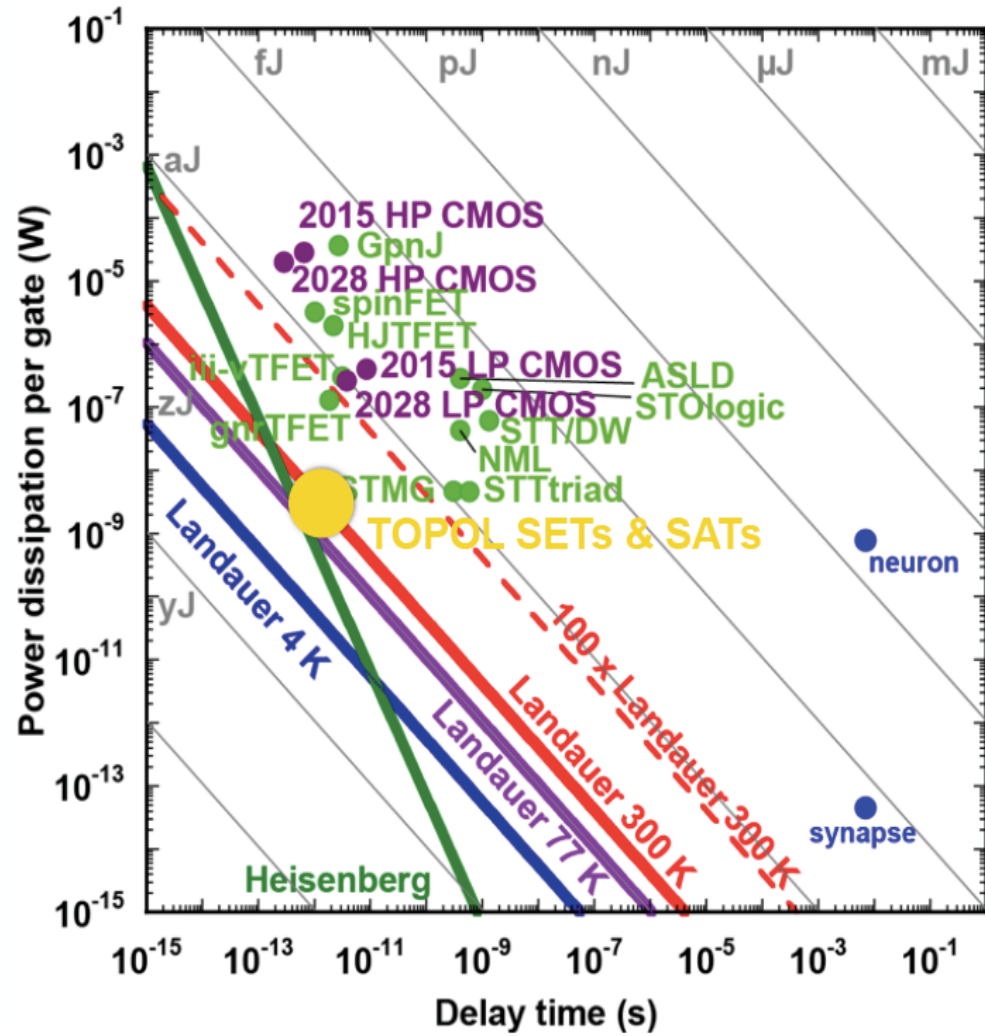
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This is not apparently the case.

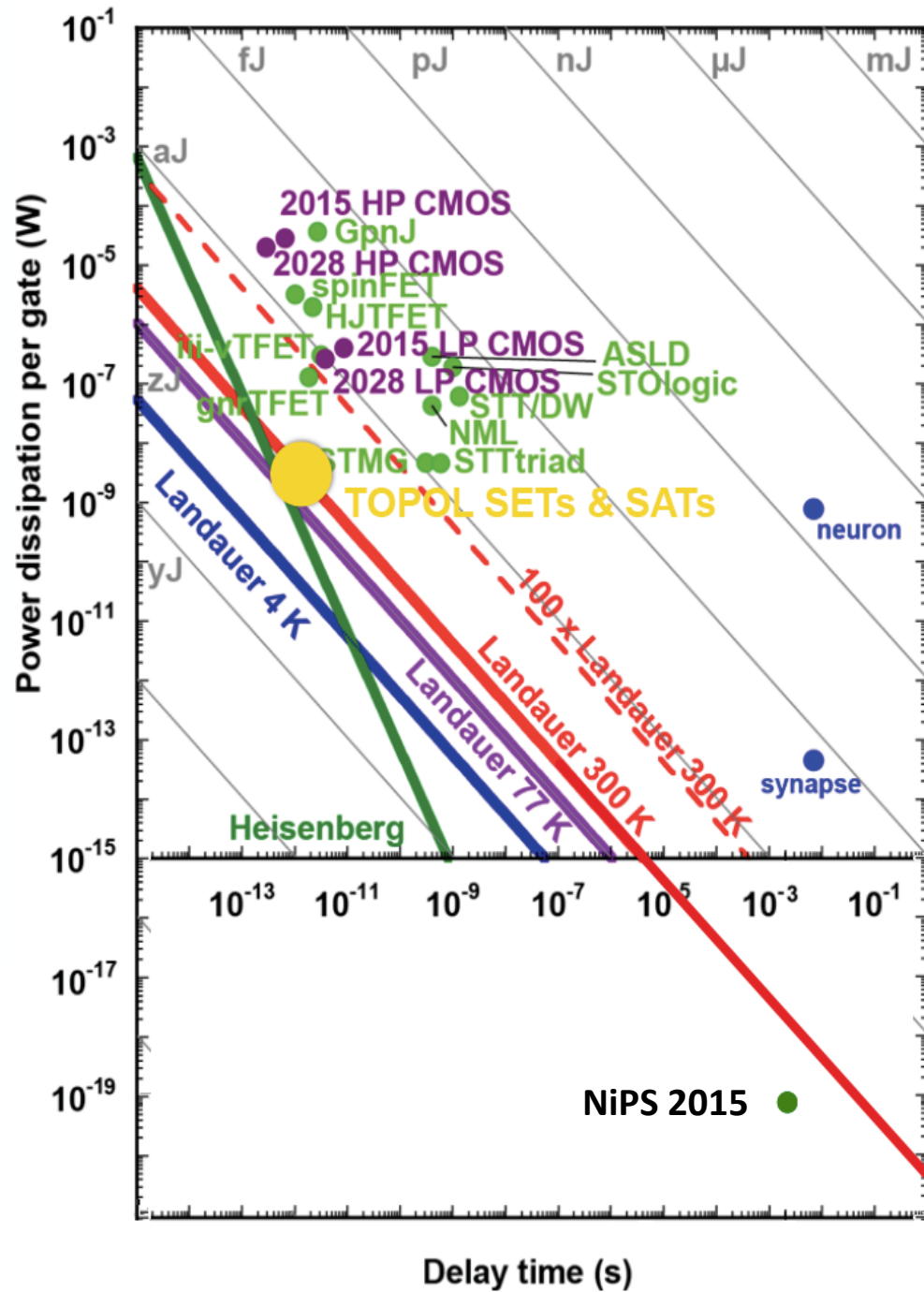
Logical reversibility is not needed in order to perform zero-dissipation computing.

The state of the art



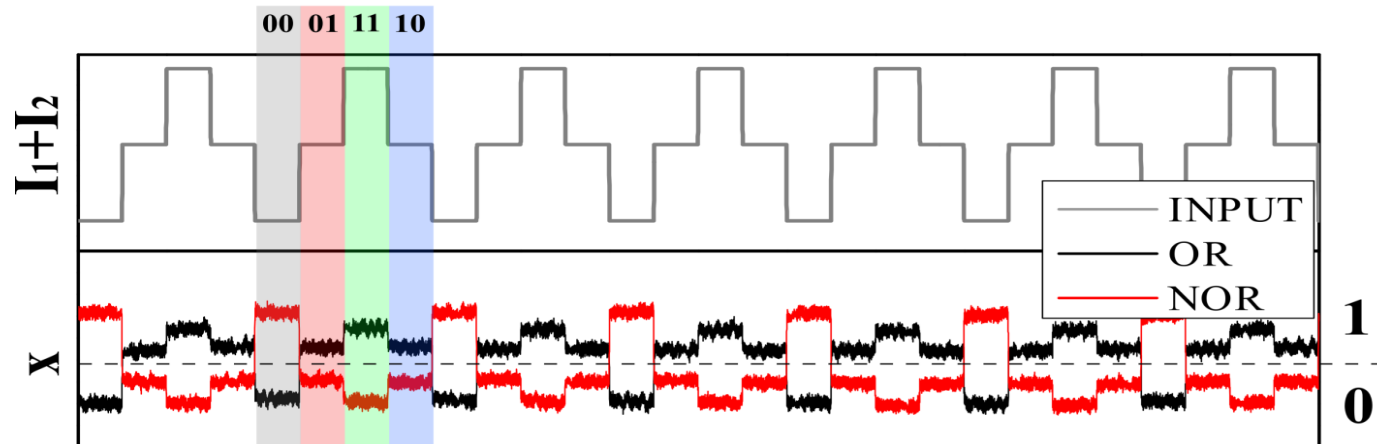
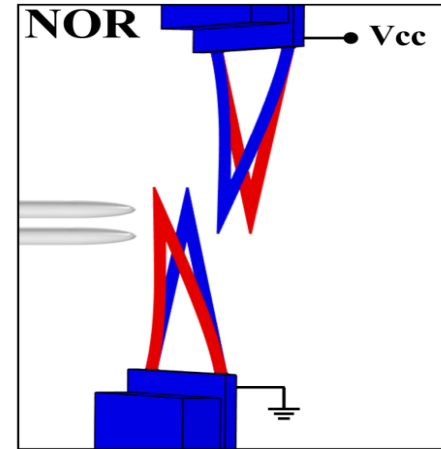
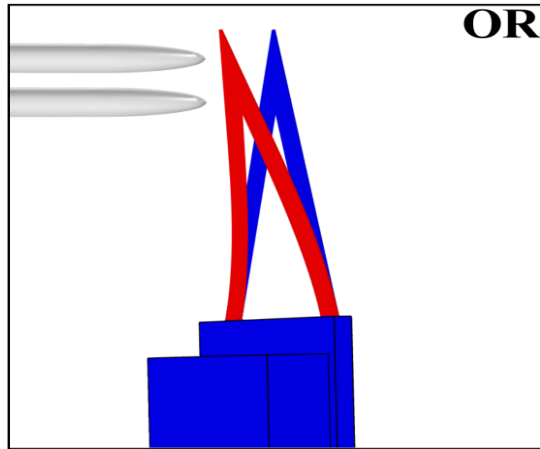
Source: D. Paul, ICT-Energy Research Agenda, 2015

The state of the art

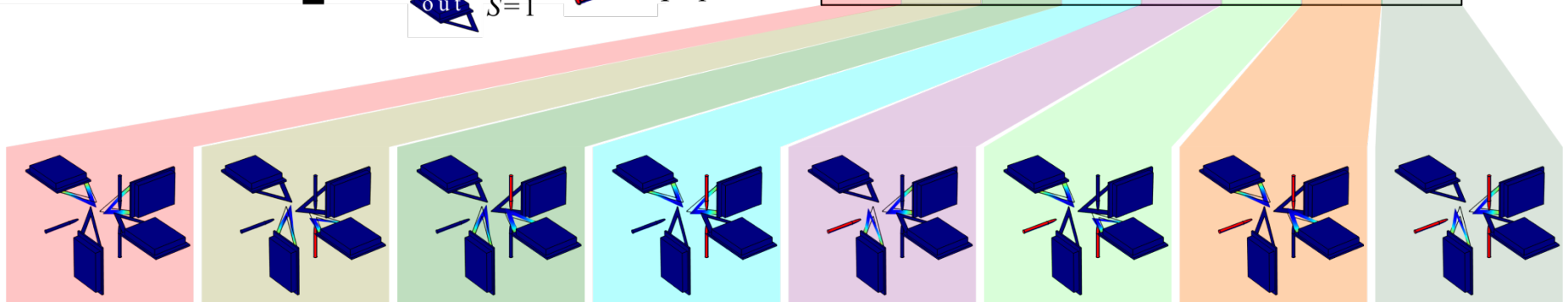
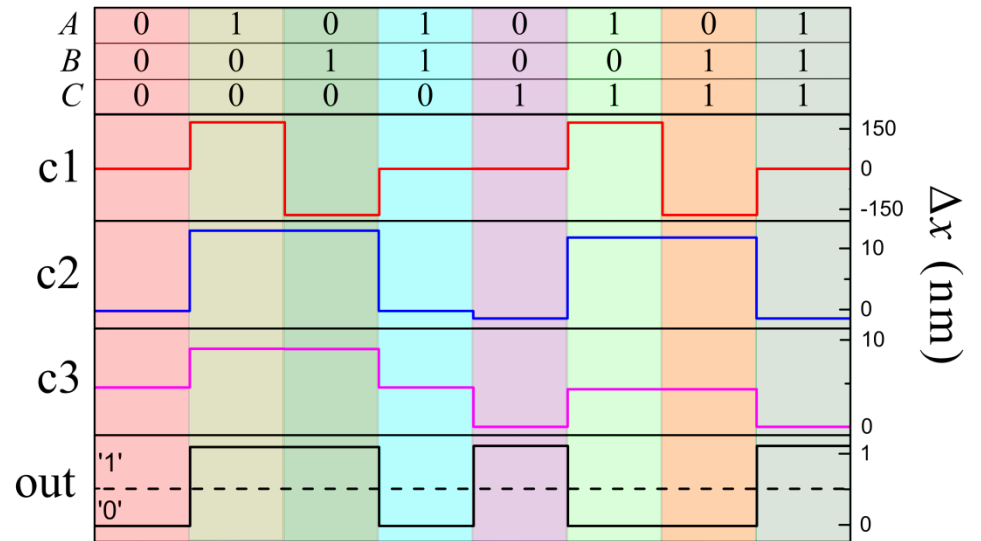
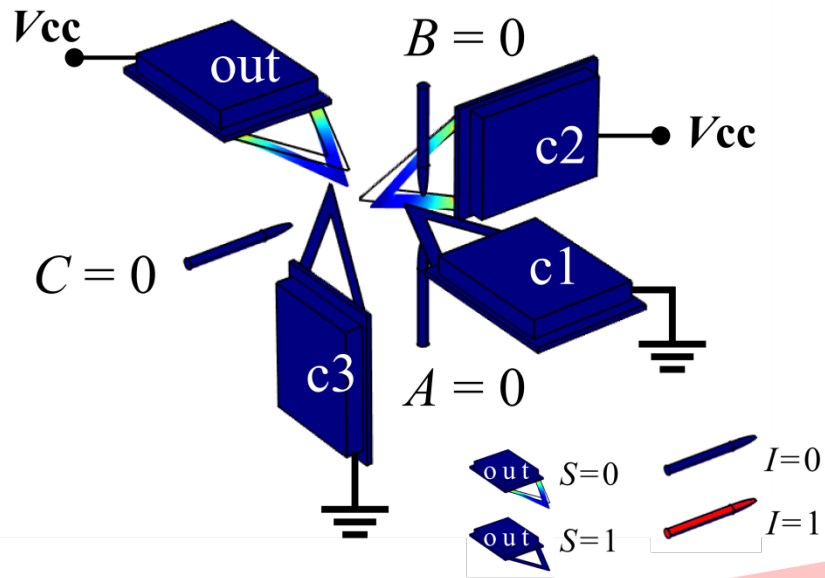


Source: D. Paul, ICT-Energy Research Agenda, 2015

Universal logic gate



One bit full adder



If you want to know more



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